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(19)



Europäisches Patentamt  
European Patent Office  
Office européen des brevets



(11)

EP 0 825 559 A2

(12)

## EUROPEAN PATENT APPLICATION

(43) Date of publication:  
25.02.1998 Bulletin 1998/09

(51) Int Cl.<sup>6</sup>: G06T 11/20

(21) Application number: 97306168.2

(22) Date of filing: 13.08.1997

(84) Designated Contracting States:  
AT BE CH DE DK ES FI FR GB GR IE IT LI LU MC  
NL PT SE  
Designated Extension States:  
AL LT LV RO SI

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(54) Method and apparatus for modifying a node-link diagram

(57) In a computer controlled display system capable of supporting free form graphical input, techniques for maintaining the topology of a node-link structure when nodes are moved (401). When a node is moved, arbitrarily shaped links to other nodes will automatically be reshaped. The manner in which links are reshaped will depend on where a node is moved relative to the node to which it is linked. Various techniques for reshaping the node in order to retain the node-link structure topology are provided. A link may be reshaped (404, 406) by curve transformation or flipping the link shape about an axis (405). Curve transformation is a technique wherein the shape characteristics of a link are retained no matter where the node is moved. However, links that intersect, i.e. pass through, the nodes may arise from such reshaping. Various techniques for correcting link intersection situations and include flipping the attachment points (409) of the links on the nodes, truncating (412) and reattaching the link at the point where a link intersects a node or rerouting the link (410) so that intersection is avoided.

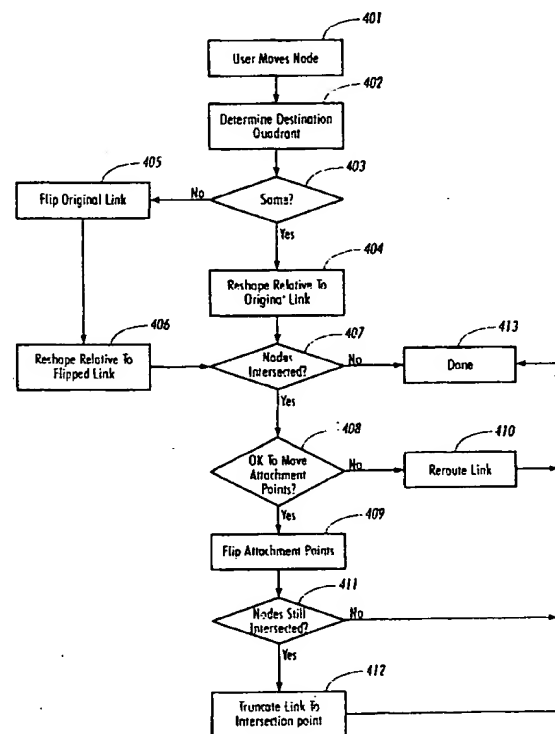


FIG. 4

## Description

The present invention is related to techniques that modify a node-link diagram.

Computer based systems such as pen based systems and "electronic whiteboards" (e.g. the LiveBoard™ available from LiveWorks, a division of Xerox Corporation), provide graphical user interfaces based on utilization of an input device such as a pen, stylus or a cursor control device. In such systems the "display" acts as both a means for showing data and as an input medium. Graphic objects may be "drawn" on the display via pen strokes created using the input device. The graphic objects may represent words, figures or anything that can be displayed. Various operations can then be performed on the graphic objects using an input technique known as gestures. Gestures are themselves merely pen strokes which are interpreted as instructions. Sometimes, such systems will have a draw mode of operation and a gesture mode of operation to distinguish when a pen stroke creates a persistent graphic object or when the pen stroke is treated as a gesture.

When interacting with a computer based system, stopping the thought process in order to wait for operations, e.g. to group or rearrange graphic objects, has a very detrimental effect. Such stoppages generally slow the creative processes. This is of particular impact to the synergy of the group interactions. Artificial delays may cause participants to "lose their train of thought" resulting in the possible loss of ideas. Thus, there is a general need in systems with graphical user interfaces for techniques that provide intuitive and quick manipulation of graphic objects.

One use of systems is the creation and manipulation of node-link diagrams. For example, various project management, flowcharting and drawing programs enable the maintenance of the topology of a node-link structure as the nodes are moved. Known programs typically operate with the nodes and links being of a known pre-declared type. Difficulties however arise when the diagram is free-form, i.e. the nodes and links have arbitrary shapes.

Such manipulation of a free form node-link structure is described in EP-A-0 667 567. EP-A-0 667 567 discloses diagrams, i.e. node-link structures, which have persistent links which maintain shape characteristics as nodes are moved. Links are reshaped using linear geometric transformations that preserve a link's characteristic shape while "stretching" enables the link to fit the new positions of the nodes it connects. Endpoints of the links may be moved if movement of the node requires it.

The invention addresses problems that arise in automatically repositioning and reshaping links. For example, if a simple geometric transformation such as scaling is performed on a link, and the link has the shape of a single period of a sine curve, the "humps" of the curve may be greatly extended, producing an undesirable distortion of the link's shape. Also, if a link is simply rotated

about a point at which it touches or attaches to a node, the link may have a counterintuitive appearance after rotation. These and various other automatic repositioning and reshaping techniques may also leave a link positioned or shaped such that it intersects a node. All of these problems may require manual correction, making automatic repositioning and reshaping less efficient.

The invention provides techniques that alleviate these problems. Some of the techniques transform segments of a link. Others flip a link about an axis. And others detect and eliminate link-node intersections.

The techniques are advantageous because they can automatically maintain a node-link diagram within which a node or other feature is moved or otherwise modified, and the techniques do so without modifying the topology of the node-link structure the diagram represents. As a result, fewer manual corrections are required to produce an acceptable node-link diagram.

In one aspect of the invention, there is provided a method for modifying a node-link diagram, said node-link diagram having a link, said method comprising: (a) receiving a request that the node-link diagram be modified; (b) in response, modifying the node-link diagram by modifying the link, the modification of the link including one or more of the following: (b1) transforming each of two or more segments of the link; (b2) flipping the link about one or more axes between a first position and a second position; and (b3) initially modifying the link, and, if the initially modified link intersects a node, further modifying the link to eliminate the intersection with the node.

In another aspect of the invention, there is provided a system comprising: input means for providing requests for modifications in node-link diagrams; processing means for responding to the requests by modifying node-link diagrams; in response to a request to modify a node-link diagram having a link, said processing means modifying the node-link diagram by modifying the link; said processing means, in modifying the link, performing one or more of the following: (A) transforming each of two or more segments of the link; (B) flipping the link about one or more axes between a first position and a second position; and (C) initially modifying the link, and, if the initially modified link intersects a node, further modifying the link to eliminate the intersection with the node.

The input means can be used to create and move free form graphic objects on a work surface whose contents are displayed by display means. The processing means can interpret graphic objects on the work surface as a node-link diagram. In transforming a link, the processing means can generate link characteristic data, flip a link about an axis, and curve transform each segment of the link based on the link characteristic data, an original location of the moved node, and a destination location of the moved node. In detecting and eliminating an intersection, the processing means can detect an intersection point and modify the link so that it attaches to

the intersected node at the intersection point.

The invention can be implemented in a program storage device that is readable by a machine and that tangibly embodies a program of instructions executable by the machine to perform the techniques described herein.

In a computer controlled display system capable of supporting free form graphical input, techniques for maintaining the topology of a node-link structure when nodes are moved are disclosed. A link will be reshaped depending on where a node is moved relative to the node to which it is linked. Both the link and node are of an arbitrary shape. In the simple case, a link will stretch or contract if the link is a straight line and direction of movement is along that line. However, links and the direction of movement of nodes are not limited to straight lines. So various methods for retaining the node-link structure topology when a node is moved are needed. Generally, the link reshaping occurs automatically when a node is moved. The intent with respect to "automatic" link reshaping is to retain the basic shape characteristics of the link and to avoid undesirable artifacts when moving a node (e.g. a link intersecting through a node). Link reshaping is accomplished through a combination of curve transformation, link flipping, link attachment point flipping and link truncation.

Curve transformation of a link is more than a simple scaling. Rather, a link is composed of a plurality of segments, and the displacement from a node move operation is divided up (according to a certain transformation factor based on each segment) and added to the segments. Flipping the link shape retains shape characteristics and is desirable since a node may be moved anywhere on a work surface relative to a stationary node. The points at which links "touch" a node are termed attachment points. The attachment points at which the link is attached to the stationary node is used to define an origin of a local coordinate system for performing the link reshaping. Depending on where the node is moved, the link shape may be flipped about one or both of the axes of the coordinate system and the flipped link image used for reshaping.

Avoiding undesirable artifacts (i.e. a link intersecting a node) is accomplished by flipping the attachment points of the link on the nodes or by rerouting the link. Flipping an attachment point is invoked only if the node permits flipping of attachment points. If flipping the attachment point does not correct the intersecting link, the link may be truncated at the point where the link intersects the node.

If attachment point flipping is not permitted, link rerouting may occur. In link rerouting, the link is redrawn to follow the outlines of the fixed and moved nodes and where the outlines are connected by a retained portion of the original intersecting link.

Finally, an intersecting link may be corrected by a user selecting an attachment point of a node and manually moving it to a new non-intersecting location on the

node.

The present invention has been implemented for use on a computer controlled display system having a graphical user interface and which utilizes an input device which allows a person to draw graphic objects for input. Examples of such systems include pen based systems, systems utilizing "paint" type programs, electronic whiteboards or electronic desk surfaces.

The invention will now be described, by way of example, with reference to the accompanying drawings, in which:

Figure 1 is a block diagram of a computer based system;

Figure 2 is a representation of a basic graphical user interface and as may be displayed on the display and interfaced through the touch sensitive panel of Figure 1;

Figure 3 is an illustration of a node being moved and corresponding link reshaped;

Figure 4 is a flowchart summarizing link reshaping;

Figure 5 illustrates the spatial coordinates of link reshaping;

Figures 6 and 7 illustrate an undesirable result of simple geometric scaling of an instance of a link;

Figure 8 is an illustration of curve sample points and segments as found in the representation of a curve;

Figure 9 is a flowchart illustrating steps for curve transformation;

Figure 10 is an illustration of the link of Figure 3 as flipped across the various axes as may be performed when a node is moved out of its original quadrant;

Figures 11-12 illustrate the moving of a node so that it causes a reshaped link to intersect a node;

Figure 13 is an illustration of flipping attachment points on a node after the movement of the nodes in Figure 11;

Figure 14 is an illustration of selecting a flipped attachment point at various points on an asymmetrically shaped node;

Figure 15 is an illustration of selecting a flipped attachment point when the node is intersected at multiple points;

Figures 16 and 17 are an illustration of a variation of flipping an attachment point by moving an attachment point across the edge of a node;

Figures 18 and 19 are an illustration of how moving a node can cause a link to intersect the node and flipping the attachment point does not correct the node intersection;

Figure 20 is an illustration of link truncation;

Figure 21 is an illustration of link rerouting to correct intersecting nodes;

Figure 22 is a flowchart illustrating the step for rerouting a link;

Figures 23-26 illustrate the steps performed in Figure 22 of rerouting a link;

Figures 27 is a flowchart illustrating the steps for creating the outline of a node boundary; and Figures 28-30 illustrate the performance of the various steps of Figure 23 for creating the outline of a node boundary.

The present invention addresses a problem that can arise when working in a free-form graphics based computer system that is capable of manipulating node-link diagrams. A node-link diagram may include a flowchart, an organization chart, a state diagram, project management charts or the like. It is often desirable to be able to move nodes around in node-link diagram while retaining the links. Also, as the node-link diagram may be created in a free-form manner so that nodes and links have arbitrary shapes, it has been determined that it is desirable that the links retain their original shape characteristics. So the present invention enables a user to modify a node-link diagram through movement of nodes without having to be concerned about altering the links.

The following terms are used in this description and have their indicated meanings:

**Graphic Object:** Any displayed object in 2D space.

**Curve:** A graphic object created manually by the user (e.g. by a pen stroke) or made by other means, such as by a gesture (e.g. a selection rectangle resulting from a selection gesture).

**Pen Stroke:** An action with a pen which becomes an ink stroke or a gesture.

**Ink stroke:** A curve that is persistent.

**Gesture:** A curve made with a pen stroke that is ephemeral and which is interpreted as an action.

**Selection:** A set of graphic objects tagged as being selected.

**Node:** A graphic object or group of graphic objects within some bounded region. Such a bounded region will typically have a visible boundary.

**Link:** An ink stroke touching or attached to one or two nodes. The link may be described as "linking" nodes. A node may also be linked to itself.

**Node-link Diagram:** A diagram that includes graphic objects that can be distinguished into nodes and links with each link linking two nodes or linking a node to itself.

**Intersect:** A link "intersects" a node when the link extends across the object or objects of the node. For example, a link that intersects a node can have an end that touches the node but, rather than extending from the end away from the node, the link can extend from the end across the node.

A computer based system as may be utilized in the present invention is illustrated with reference to Figure 1. Referring to Figure 1, the computer based system is comprised of a plurality of components coupled via a bus 101. The bus 101 illustrated here is simplified but

any appropriate bus architecture could be used to implement the present invention. The bus 101 may consist of a plurality of parallel buses (e.g. address, data and status buses) as well as a hierarchy of buses (e.g. a processor bus, a local bus and an I/O bus). In any event, the computer system is further comprised of a processor 102 for executing instructions provided via bus 101 from Internal memory 103 (note that the Internal memory 103 is typically a combination of Random Access or Read Only Memories). When in operation, program instructions for carrying out the various functional components described herein are stored in internal memory 103. The processor 102 and Internal memory 103 may be discrete components or a single integrated device. The processor 102 and internal memory 103 comprise circuitry, software, or other means for performing the various processing functions described herein. Also coupled to the bus 101 is external storage 107. The external storage 107 typically includes high capacity storage media such as magnetic or optical disk storage.

Also coupled to the bus 101 is a display 104 and a pointing device 105. In one embodiment, the pointing device 105 is a pen driven touch sensitive panel which is integrated with the display 104 as a touch screen display. Such touch screen displays are well known in the art and are utilized in such systems as Pen based system and for electronic whiteboard systems. However, the pointing device 105 and display 104 need not be integrated so that the pointing device 105 may also be a stylus, mouse, track-ball or other cursor control device.

Figure 2 illustrates a particular implementation of a graphical user interface. Referring to Figure 2, the graphical user interface is displayed on display 104 and interacted with via touch panel 105. The graphical user interface employs a working surface and may employ a plurality of accessible functions 201 as is shown. The working surface 202 is where a user may draw various curves and where other graphic objects are displayed. The accessible functions 201 are positioned at the button area 203 of the display. The functions 201 may include operations for editing graphic objects (create, delete, move, shrink, etc.) or changing the operating mode of the touch panel 103 (e.g. switching from draw and gesture mode).

These functions may alternatively be accessed by pull down menus that are commonly found in Windows oriented applications. These functions however are optional in designation, their principal objects being to define operations which are inherent in the operation of the system. These functions may perform the same functions that are invoked by gestures.

One embodiment of the present invention is implemented on a pen based system having a Graphical User Interface (GUI). Such a GUI will typically support operations such as "tap" for selecting/deselecting a graphic object or "double tap" for invoking an operation that may be associated with the graphic object being tapped on. Once an object is selected it may be dragged and

dropped to a desired location in the work space. As will be described in greater detail below, such a tap gesture will cause an outlining of the selected graphic object, e. g. a node in a node-link diagram, to be outlined and displayed in a visually distinct manner. This outlining provides the user with feedback that the graphic object has been selected.

The work space of one embodiment permits graphic objects that are made "freehand". Hence nodes and links may have an arbitrary shape. This is consistent with how a whiteboard is used.

One embodiment of the present invention has been implemented using software programs in the C++ programming language, for use on a pen based system, such as the LiveBoard, running under the control of a suitable whiteboard emulation program. Such software programs may be stored on a suitable storage medium such as magnetic diskettes or CD-ROMs.

Node-link diagrams have many uses. They may be used to describe a process flow, or to show relationships between grouped items. The organization and relationship between nodes and links is referred to as the "topology" of the node-link diagram. It is desirable when manipulating the spatial position of nodes that the topology is retained.

A node in a node-link diagram may have an arbitrary shape and may represent a group of related graphic objects. These graphic objects may typically represent letters, words or other information conveying symbols. A node may be represented by the encircling of graphic objects with an ink stroke or by any grouping means. A node may have a visible boundary which indicates the spatial limits of the node. A node may have multiple links to other nodes. Selection of a node may also cause selection of its links.

Links are ink strokes that are used to provide a visual connection between one or more nodes. Links may also have an arbitrary shape. Providing links between nodes is useful, particularly when repositioning the nodes. Being able to retain the visual association between the nodes even as they are moved helps provide unencumbered usage of the graphics based system.

A link is created by simply drawing a curve that "touches" at least one node. By touching a node it is meant that an appropriate criterion for touching or nearness is met. For example, if a link has an endpoint and a node has a boundary, the criterion could require that the link endpoint be within a predetermined distance of the node boundary. The point at which a link "touches" a node is termed an "attachment point". Links are associated with at least one node (i.e. one-ended) and at most two nodes.

One embodiment can handle multiple nodes and links, but the basic problems resulting from links can be understood from the node-link diagram illustrated in Figure 3. Figure 3 shows a single link L1 301 with a node at each end, a stationary node N 302 and a node N1 303 that the user moves manually to a position labeled

as N2 304. As a result of this move the link L1 301 is reshaped to be the link shown as L2 305. The attachment points of the link to the nodes are shown as A 306, A1 307, and A2 308.

Figure 4 is a flowchart which overviews link reshaping as may be performed in one embodiment of the present invention. Referring to Figure 4, first a user moves a node in a node-link diagram, step 401. This can be performed by a simple drag and drop operation or by any operation supported by the underlying graphical user interface. The first step in reshaping the node and links is to identify the destination quadrant, step 402. A determination is made if the destination quadrant is the same, step 403. Determination of the destination quadrant will indicate if flipping of the original link is required. If the destination quadrant is the same, curve transformation for the link occurs relative to the original link, step 404. If the destination quadrant is not the same, the original link is flipped across the respective axes to the destination quadrant, step 405. Curve transformation for the link is then performed relative to the flipped link, step 406.

After the link has been reshaped, it is determined if any of the nodes are intersected by the reshaped link, step 407. If no links intersect a node, then the link reshaping is completed, step 413. If links do intersect a node, it is determined if attachment points of the nodes may be moved, step 408. If they cannot, link rerouting may be performed, step 409. Otherwise, the attachment points to the nodes are rerouted, step 410. A check is then made to determine if an intersection still exists, step 411. If no nodes are intersected after the attachment points are flipped, the link reshaping is completed, step 413. If a node remains intersected by a link, the link is truncated at the point in which a node is intersected, step 412. Upon completion of truncation, the reshaping of the link is completed, step 413.

It should be noted that in one embodiment attachment points may be selected and moved by the user. This is necessary since the user may want to alter the relationship between the nodes. Further, the user may want to do this if the user is not satisfied with the results of an automatic link reshaping.

As noted above, a link is an instance of a curve. Curve transformation can be conceptually thought of as the stretching or contraction of a link so that it retains its shape characteristics. For curve transformation, the link is considered in isolation, as shown in Figure 5. Link L1 301 goes from A 306 to A1 307. It is desirable that the link L2 305, which goes from A 306 to A2 308, have the same shape characteristics as L1 301. It should be noted that in this representation the attachment point A 306 of the fixed node is placed at the origin of a two-dimensional coordinate system. So attachment point A1 307 is at coordinates (x1 501, y1 502) and attachment point A2 308 is at coordinates (x2 503, y2 504). The objective is to transform the remainder of the curve so that the shape characteristics of L1 301 are retained.

One way of performing a transformation is a simple geometric transformation (e.g. scaling). However, it has been determined that this causes undesirable results in certain situations. Such an instance is illustrated in Figures 6 and 7. Referring to Figure 6, a link 601 in the shape of a single period of a sine curve is attached to node 602 and 603. A simple geometric transformation is typically given by the following: The x-y coordinates of the original attachment point are  $\langle x1, x2 \rangle$  and  $\langle x2, y2 \rangle$  for the attachment point as moved. To transform the link, every point  $P\langle x, y \rangle$  on the link is moved to  $P'\langle x', y' \rangle$ , where  $x' = x * x2/x1$  and  $y' = y * y2/y1$ . Note that in some cases the denominator may be small or even zero. The result is illustrated in Figure 7. Referring to Figure 7, as a result of moving node 603 the link 701 is transformed so that "humps" 702 and 703 of the curve are greatly extended. This is a result of the denominator being a small fractional number. Thus, a different approach for reshaping the link could be used to solve this problem.

To better understand how curve transformation occurs, an understanding of how a curve is represented is necessary. The simplest way to represent a curve is by its set of sample points. These are naturally ordered by their order of input. Some systems represent a curve directly by a bitmap, or a bitmap generated by fitting a curve(spline) through the sample points. In the currently preferred embodiment, a curve is represented by its starting point and its set of segments, where a segment is the vector  $\langle dx, dy \rangle$  determined by two consecutive sample points. This is illustrated in Figure 8. Referring to Figure 8, a curve 801 appears on a work surface. The curve 801 is detected by the samplings which occurred at points 810-820. The distance between sample points is termed a segment. For example, a segment 831 is defined between sample points 810 and 811 where sample point 811 is the end sample point. For convenience, the curve is normalized by orienting it so that the fixed attachment point is the starting point and the moved attachment point is the ending point of the curve.

The curve transformation technique of the illustrated embodiments takes the difference between the before and after attachment points and distributes this onto the segments of the curve. In other words, the points making up the link are transformed to new locations so that the shape of the original link is maintained. The technique is described with reference to the flowchart of Figure 9 and the coordinate points described in Figure 5. Referring to Figure 9, the first step is to calculate total X and Y displacements, step 901. Let  $(x1, y1)$  and  $(x2, y2)$  be the before and after positions of the moved attachment point of the link. Then:

$$xDisp = x2 - x1,$$

$$yDisp = y2 - y1.$$

The remaining steps are then carried out for each of the segments of the link. For the i-th segment  $\langle dx[i], dy[i] \rangle$ , the transformation is calculated, as described in steps 902-904, resulting in a new i-th segment  $\langle Tdx[i], Tdy[i] \rangle$ . This is performed by the following calculation:

First the x and y arclengths of the curve are computed, step 902:

$$x\text{-arclength} = \sum |dx[i]|,$$

$$y\text{-arclength} = \sum |dy[i]|,$$

where  $|x|$  denotes the length or absolute value of x.

Then the transformation factors  $cx[i]$  and  $cy[i]$  are calculated based on the x and y lengths of the i-th segment, step 903:

$$cx[i] = |dx[i]| / (x\text{-arclength}),$$

$$cy[i] = |dy[i]| / (y\text{-arclength}).$$

Now the contributions of the displacement to be added to the i-th segment are given by  $cx[i]*xDisp$  and  $cy[i]*yDisp$ , so the new i-th segment, is computed by, step 904:

$$Tdx[i] = cx[i]*xDisp + dx[i],$$

$$Tdy[i] = cy[i]*yDisp + dy[i].$$

Note in the examples in Figures 3 and 5 that attachment points A1 and A2 are in the same quadrant of the coordinate system defined where attachment point A is the origin. In one embodiment, besides being reshaped, if A2 is in a different quadrant than A1, then the link shape can be flipped (mirror-reversed) around the x-axis, the y-axis, or both. This flipping is a desirable visual property, since this is what the user naturally expects. Figure 10 shows these three cases of flipping. If A1 were moved from quadrant 1001 to quadrant 1002, the result would be A4 1007. The flipping would occur about the y-axis 1006. If A1 were moved from quadrant 1001 to quadrant 1003, the result would be A5 1008. The flipping would occur about the y-axis 1006 and the x-axis 1005. Finally, if A1 were moved to quadrant 1004, the result would be A3 1009. The flipping would occur about the x-axis 1005.

Generally, when movement out of the quadrant occurs, what first occurs is the flipping of the link to the destination quadrant. Flipping the link shape is accomplished by a simple geometric transformation to the desired quadrant. This is followed by the link reshaping de-



scribed above performed relative to the flipped link.

Having transformed the shape of the link, this is all that needs to be done in the simple case shown in Figure 3. But Figures 11 and 12 illustrate a case where the reshaping and flipping have created undesirable results. Referring to Figure 11, node N1 1101 with attachment point A1 1102 is moved to a position denoted as N2 1103 with attachment point A2 1104. Fixed node N 1105 has attachment point A 1106. Link L1 1107 links node N 1105 with node N1 1101. The result of this after link reshaping and flipping is shown in Figure 12. The link L1 1107 has been reshaped to link L2 1201, and L2 1201 intersects both node N 1101 and node N2 1103. This is surely not what the user wants. Thus, techniques for adjusting the attachment points to obtain satisfactory results are needed.

A first step in correcting node intersection is to just flip the attachment points of the link. There are two cases of flipping -- across a node or along an edge. In flipping an attachment across a node, the flipping occurs to the opposite side of the node. The results of applying this technique to the example in Figures 11-12 is shown in Figure 13, where attachment points A and A2 in Figure 13 are moved to A' 1301 and A2' 1302. With respect to maintaining the topography and visual results, this provides quite satisfactory results. However, it is recognized that in some instances the node shape has a meaning such that a relationship between nodes will be interpreted differently depending on where a link is attached. For example, attachment on one side indicates an input and attachment on the opposite side indicates an output. Thus, internal node representations will contain some indicator, such as a flag or a node type, which may be used to indicate whether or not the flipping of attachment points is permitted.

Flipping attachment points is straightforward in the case where the node shape is nearly symmetric about the axis of flip. So consider the asymmetric case. Only the case of left-right flipping about the vertical axis is considered; the other cases are similar. The asymmetric case is illustrated in Figure 14. Referring to Figure 14, an asymmetrically shaped node 1405 is shown. To flip a point A1 1401 from right to left a horizontal line is drawn from A1 1401 to the other side of the node 1405 until it intersects the node at A1' 1403, which is the new attachment point. Note that in an asymmetric case the flipped points can be quite different. For example, both A1 1401 and A2 1402 are on the far right of the node, and the flipped point A2' 1404 is on the far left of the node 1405, but flipped point A1' 1403 is in the middle of the node 1405.

Another case to consider is where the horizontal line intersects the node enclosure in more than two places. It is then important to pick the corresponding point to flip to. This case is illustrated in Figure 15. Referring to Figure 15, points A1 1501 and A1' 1502 correspond as flip points and points A2 1503 and A2' 1504 correspond as flip points. To identify the corresponding flip

point, number the intersection points going from left to right. Determine the number I of the current attachment point (i.e. the attachment point is the Ith from the left). Now number the points going from right to left. The corresponding point is the Ith point from the right.

Flipping an attachment point along the edge of a node occurs when movement of the node is parallel to the node edge having the attachment. Further, the beginning and ending location of the nodes must be such that there is no overlap. Flipping an attachment point across the edge of a node is illustrated in Figures 16 and 17. Flipping an attachment point across an edge may occur on one node while flipping across the node may occur across the other node. Referring to Figure 16, nodes 1601 and 1602 are linked via links 1603 and 1604. Link 1603 is attached to node 1601 at attachment point 1605 and to node 1602 at attachment point 1606. Link 1604 is attached to node 1601 at attachment point 1607 and to node 1602 at attachment point 1608. Referring now to Figure 17, the node 1601 has been moved to a new position wherein the attachment points 1606 and 1607 are flipped across nodes 1602 and 1601, respectively, to attachment points 1606' and 1607'. Meanwhile the attachment points 1605 and 1608 have been flipped across the edge of their respective nodes 1601 and 1602 to attachment points 1605' and 1608'. Note that the links 1603 and 1604 have been reshaped to links 1603' and 1604' and retain their basic shape characteristics.

The flipping of an attachment point along an edge is accomplished by finding a center point of the edge, finding a distance X between the center point and the attachment point, and flipping the attachment point to a location a distance X on the opposite side of the center point.

Even when these techniques are applied, the link can still intersect a node. This is illustrated in Figures 18-19. Referring to Figure 18, node 1801 is connected to node 1802 via link 1803. Link 1803 is attached to node 1801 at attachment point 1804 and to node 1802 at attachment point 1805. Figure 19 illustrates the results of moving node 1802. Referring to Figure 19, the link 1803 has been reshaped and is illustrated as link 1803'. It is noted that the link 1803' intersects the node 1802 at point 1901. Point 1805' indicates where attachment point 1805 would be flipped. However, it is clear that even the flipping of the node would not correct the intersecting link (as illustrated by the dotted line 1902 which indicates the effect of attachment points flipping). Thus, a further "unintersection" technique is required.

To truncate a link from a node, simply find where the link intersects the node and then make that the attachment point. When a link is truncated, the overall shape of the link changes because the truncated portions are discarded. In the currently preferred embodiment, the link 1803' is truncated at intersection point 1901, deleting the segment of the link from intersection point 1901 to attachment point 1805. The result is shown

in Figure 20 wherein the reshaped link is illustrated as link 2001.

Note that in cases where there are multiple intersection points of a link on a node, the intersection point that is closest to the attachment point of the fixed node is chosen. Further, note that an alternative to truncating the link would be to curve transform the link at the point the link intersected the node.

Link rerouting is performed when an attachment point is not to be moved (flipped) and a node intersection occurs. An example of link rerouting is illustrated in Figure 21. Figure 21 illustrates a link rerouting that may be used to correct the node intersecting link of Figure 12. Referring to Figure 21, rerouted link 2101 has been rerouted to avoid the intersection with the node. Dashed line 2102 indicates where the link was originally after reshaping. The rerouted link 2101 follows the shape of the node 1105 from the attachment point 1106 to a point 2103 where it meets up with intersecting link 2102. Then the rerouting follows the shape of the link 2102 up to where it would intersect node 1103 (i.e. point 2104). From there the route follows the shape of node 1103 to the attachment point 1104.

Figure 22 is a flowchart illustrating the steps of a simple technique for rerouting a link. It is assumed that an intersecting link has been generated. First, an outline of each of the nodes is generated, step 2201. A description of how node outlines are generated is provided below with respect to Figures 27-30. In any event, this is illustrated in Figure 23 where outlines 2301 and 2302 of nodes 1103 and 1105 respectively, are illustrated. Also shown in Figure 23 is intersecting link 2303.

Next, starting from the attachment point of the fixed node, a route following the outline and having the shortest distance to the intersecting link is chosen, step 2202. This is illustrated in Figure 24. Note that the portions of outline 2302 and intersecting link 2303 that have not been used have been discarded.

The route then follows the intersecting link until it reaches the point where the outline of the moved node is intersected and the remainder of the intersecting link discarded, step 2203. This is illustrated in Figure 25 where the portion of the link 2303 intersecting node 1103 are discarded.

At this point the route follows the shape of the moved node in the direction so that the attachment point of the moved node is reached in the shortest distance, step 2204. This is illustrated in Figure 26 wherein the portions of the outline 2301 that are not used are discarded.

Finding the outline of the boundary of an arbitrarily shaped node is a non-trivial task. For an arbitrarily shaped closed curve representing the boundary, there is difficulty in determining whether a point lies on the inside or outside of the curve. The technique for finding an outline is described by the flowchart of Figure 27. Referring to Figure 27, a first outline is drawn from a starting point on one side of a boundary and a second

outline is drawn from the starting point on the opposite side of the boundary, step 2701. It is necessary to draw outlines on both sides of the boundary since it is not readily known where the curve started from and so it is unclear which is the "inside" or "outside" outline. In any event, each of the outlines is drawn the same predetermined distance from the boundary. This is illustrated in Figure 28 where an outside outline 2801 and an inside outline 2802 are shown. It should be noted that what effectively occurs is the drawing of outlines on the inside and outside of the node boundary.

Next, the outlines are converted into simple closed curves, step 2702. This is accomplished for each of the outlines by trimming small pieces at the end of the resulting curves. Such smaller curves are illustrated in Figure 28 by the curve 2803 of outline 2801 and curve 2804 of outline 2802. These curves arise by the outlining process. The discarding of these smaller curves is illustrated in Figure 29 as outlines 2801' and 2802'.

Finally, the longer of the outlines is selected as the outline for the node, step 2703. Determining the longer of the outlines is accomplished by simply summing the distances of the various segments of the two outlines and then comparing the sums. The longer of the outlines will clearly be the "outside" outline for the node. This is illustrated in Figure 30.

It should be noted that the outlining process described above is used for more than link rerouting. In one embodiment, the same outlining process is used to indicate selection of a node. This is done by highlighting or coloring the outline curve to give visual feedback to the user that the node enclosed by the outline is selected.

Thus, methods and apparatus for modifying a node-link diagram have been disclosed.

A pen based system has been described with a whiteboard emulation program and with a graphical user interface interacted with via a touch panel. The invention could be implemented in other types of systems running other types of programs and with other types of user input devices.

A criterion for touching has been described which requires a link endpoint to be within a predetermined distance of a node boundary. The invention could be implemented, however, with other criteria, with links whose ends are not points, and with nodes that do not have defined boundaries.

Automatic link repositioning and reshaping techniques have been described for individual links in response to requests to move nodes, but the techniques of the invention could be applied in response to other requests to modify a node-link diagram, such as a request to move an attachment point as described above. Further, the techniques could be applied concurrently to all links that touch a moved node or that are affected by a modification of the node-link diagram.

Link flipping techniques have been described that perform mirror-reversals across the x-and y-axes be-

tween quadrants, but flipping techniques that perform mirror-reversals across any appropriate axis could be used.

## Claims

1. A method for modifying a node-link diagram, said node-link diagram having a link (301: 801: 1107: 1603: 1803), said method comprising:

(a) receiving a request that the node-link diagram be modified:

(b) in response, modifying the node-link diagram by modifying the link, the modification of the link including one or more of the following:

(b1) transforming each of two or more segments (831) of the link (801):

(b2) flipping the link about one or more axes (1005, 1006) between a first position and a second position: and

(b3) initially modifying the link (1107: 1803), and, if the initially modified link (1201: 1803: 2102) intersects a node (1103, 1105: 1802), further modifying the link to eliminate the intersection with the node.

2. A method according to claim 1 in which the link (301: 801: 1107: 1603: 1803) is attached to a first node (302: 1105: 1602: 1801) at a first attachment point (306: 810: 1106: 1606, 1608: 1804) and to a second node (303: 1101: 1601: 1802) at a second attachment point (307: 820: 1102: 1605, 1607: 1805):

in which the request is to move the second node:

in which the method comprises, before (a):

(c) storing link shape information, said link shape information including link segment information:

in which (b) comprises:

(b4) identifying a third attachment point (308: 1104: 1605', 1607': 1805') for the moved second node (304: 1103: 1601), the third attachment point at the same location on the moved second node as the second attachment point: and

(b5) generating link displacement data for the link based on the stored link shape information: and

in which (b1) comprises:

(b1a) transforming each segment (831) of the link whereby the link is curve transformed, said transforming of each segment comprising:

(b1a1) determining an arclength for said segment:

(b1a2) determining transformation factors based on the length of said segment and said arclength for said segment:

(b1a3) determining a transformed segment location and length based on said transformation factors, link displacement data, and the original segment endpoint location (811-820): and

(b1a4) displaying said transformed segment between said transformed segment endpoint location and a previous transformed segment endpoint.

3. A method according to claim 2 in which (b5) further comprises:

(b5a) defining an X-Y coordinate system having said first attachment point (306: 810: 1106: 1606, 1608: 1804) as an origin: and

(b5b) determining displacement values in X and Y dimensions based on said second (307: 820: 1102: 1605, 1607: 1805) and third (308: 1104: 1605', 1607': 1805') attachment points.

4. A method according to claim 3 in which (b1a2) further comprises:

(b1a2a) determining the length of said segment (831) in the X dimension:

(b1a2b) determining the X-arclength of said segment as the length of said link (301: 801: 1107: 1603: 1803) up to said segment in the X dimension:

(b1a2c) calculating an X dimension transformation factor based on the ratio between said length of said segment in the X dimension and said arclength of said segment in said X dimension:

(b1a2d) determining the length of said segment in the Y dimension:

(b1a2e) determining the Y-arclength of said segment as the length of said link up to said segment in the Y dimension: and

(b1a2f) calculating a Y dimension transformation factor based on the ratio between said length of said segment in the Y dimension and said arclength of said segment in said Y dimension.

5. A method according to claim 1 in which the link (301: 801: 1107: 1603: 1803) is attached to a first node (302: 1105: 1602: 1801) at a first attachment point (306: 810: 1106: 1606, 1608: 1804) and to a second node (303: 1101: 1601: 1802) at a second attachment point (307: 820: 1102: 1605, 1607: 1805), in which the request is to move the second node, and

in which (b) comprises:

(b6) defining said first attachment point as an origin point for a coordinate system for reshaping said link:

(b7) determining a third attachment point (308: 1104; 1605; 1607; 1805) based on said moved second node (304: 1103; 1601):

(b8) determining the quadrants for said second attachment point and said third attachment point: and

(b9) if the quadrant for said second attachment point and said third attachment point are the same, curve transforming said link responsive to moving said second node based on the shape characteristics of the original link:

(b10) if the quadrant for said second attachment point and said third attachment point are different, reshaping said link, performing (b2), comprising:

(b2a) flipping said link to said quadrant of said third attachment point: and

(b2b) curve transforming said link based on the shape characteristics of said flipped link.

6. The method as recited in claim 5 in which (b3) comprises:

(b3a) detecting that a curve transformed link (1201) intersects either said first node (1105) or said second node (1103):

(b3b) determining that said first node and said second node may flip attachment points:

(b3c) determining corresponding flip attachment points (1301; 1302) for said first attachment point (1106) and said third attachment point (1104): and

(b3d) modifying said link (1201) to attach to said flip attachment point for said first attachment point and said flip attachment point for said third attachment point.

7. A method according to claim 5 in which (b3) comprises:

(b3e) detecting that a curve transformed link (1803) intersects either said first node (1801) or said second node (1802):

(b3f) identifying an intersection point (1901): and

(b3g) modifying said curve transformed link to attach to said moved second node at said intersection point by truncating said curve transformed link.

8. A method according to claim 5 in which (b3) comprises:

(b3h) detecting that a curve transformed link (2102) intersects either said first node (1105) or said second node (1103):

(b3i) determining that said first node and said second node may not flip attachment points: and

(b3j) rerouting said curve transformed link so that neither said first node or said second node is intersected.

9. A method according to claim 8 in which (b3j) comprises:

(b3j1) drawing an outline (2302, 2301) of said first node (1105) and said second node (1103): (b3j2) determining a first route part from said first attachment point (1106) to said curve transformed link (2102) based on said outline (2302) of said first node:

(b3j3) determining a second route part from said third attachment point (1104) to said curve transformed link based on an intersection point (2104) of said curve transformed link and said outline of said second node: and

(b3j4) providing said rerouted link as said first route part, said second route part and a portion (2303) of said curve transformed link connecting said first route part and said second route part.

10. A system comprising:

input means (105) for providing requests for modifications in node-link diagrams:

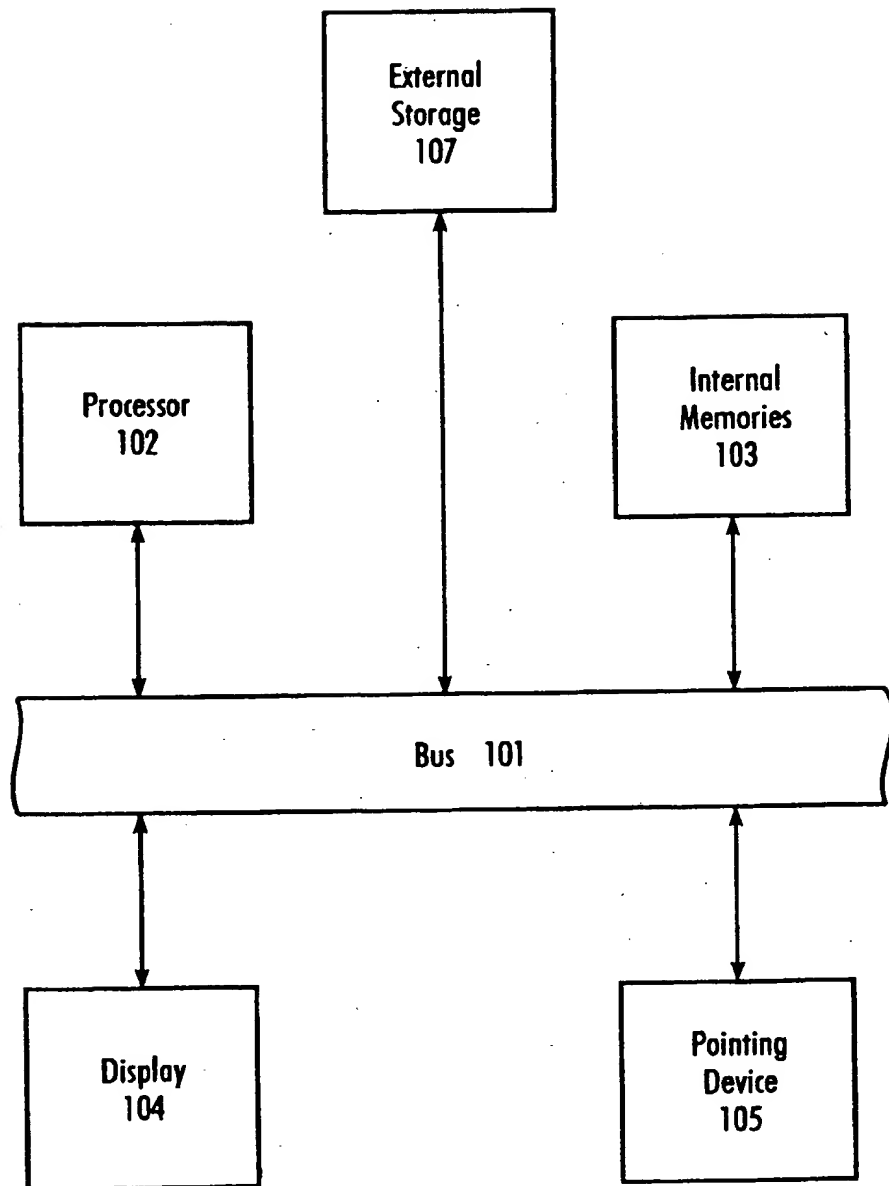
processing means (102) for responding to the requests by modifying node-link diagrams:

in response to a request to modify a node-link diagram having a link (301; 801; 1107; 1603; 1803), said processing means modifying the node-link diagram by modifying the link: said processing means, in modifying the link, performing one or more of the following:

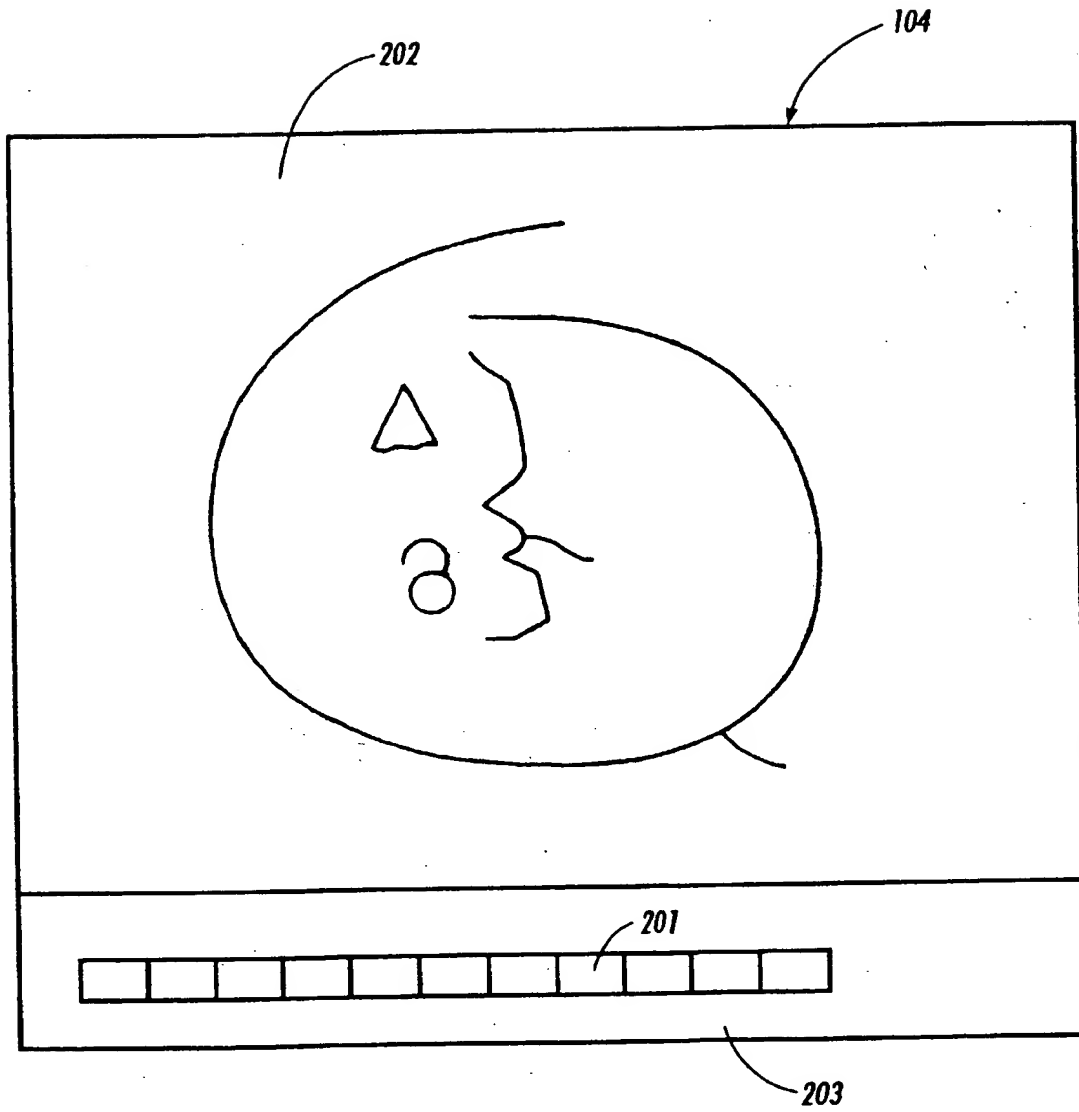
(A) transforming each of two or more segments (831) of the link (801):

(B) flipping the link about one or more axes (1005, 1006) between a first position and a second position: and

(C) initially modifying the link (1107; 1803), and, if the initially modified link (1201; 1803; 2102) intersects a node (1103; 1105; 1802), further modifying the link to eliminate the intersection with the node.



**FIG. 1**



**FIG. 2**

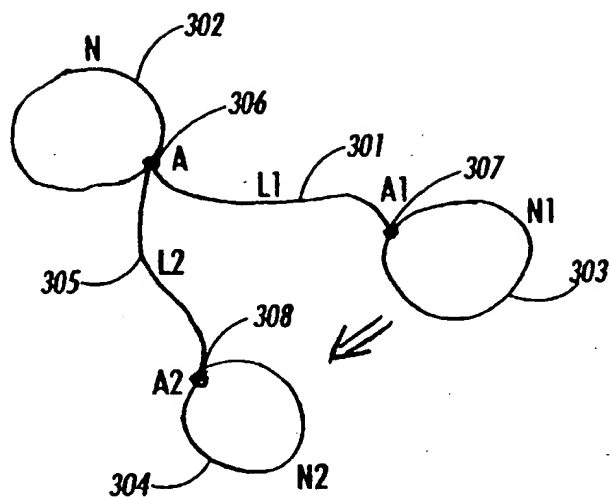


FIG. 3

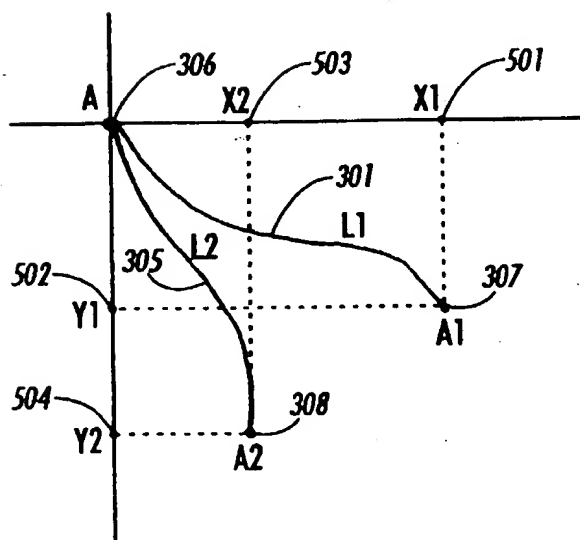


FIG. 5

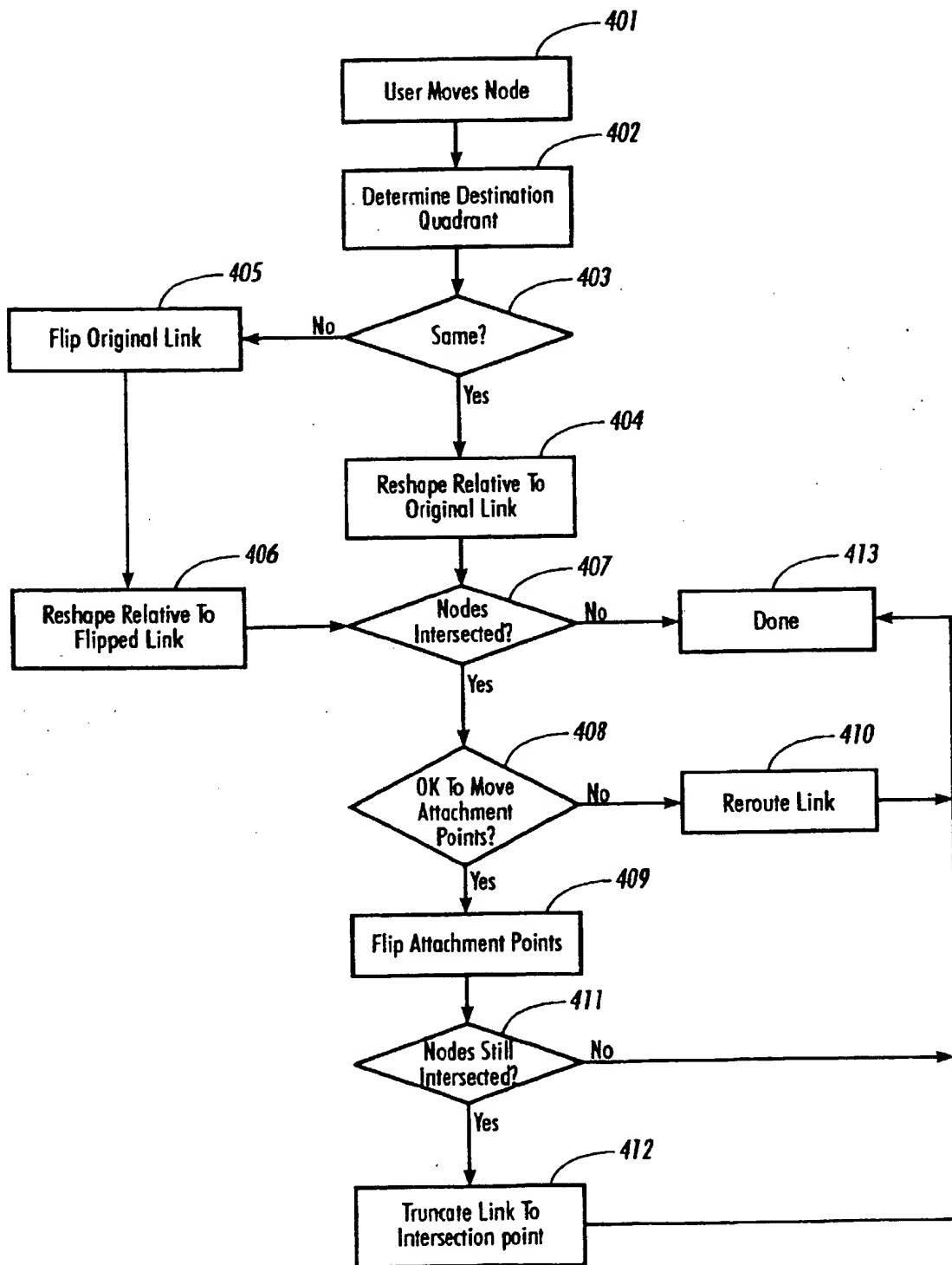
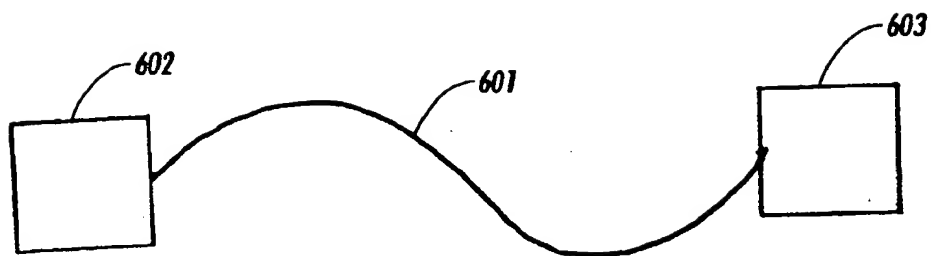
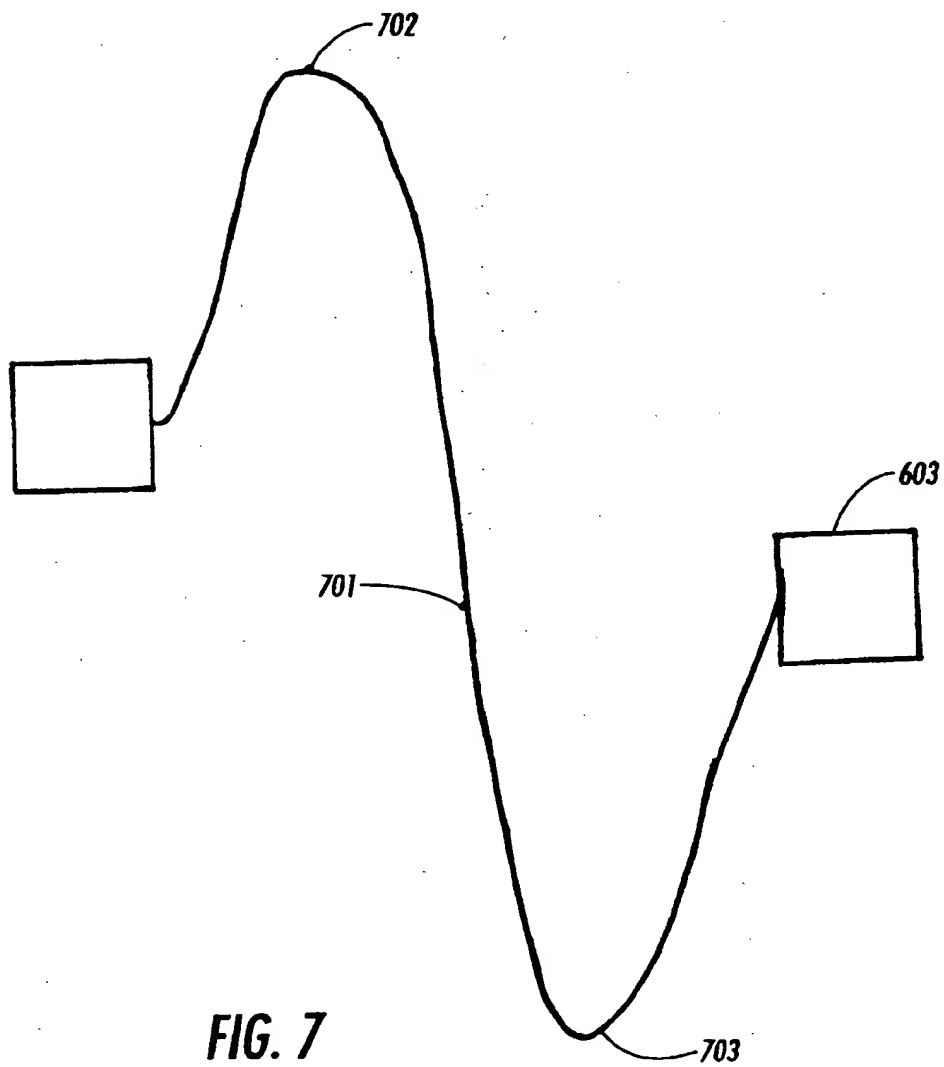


FIG. 4

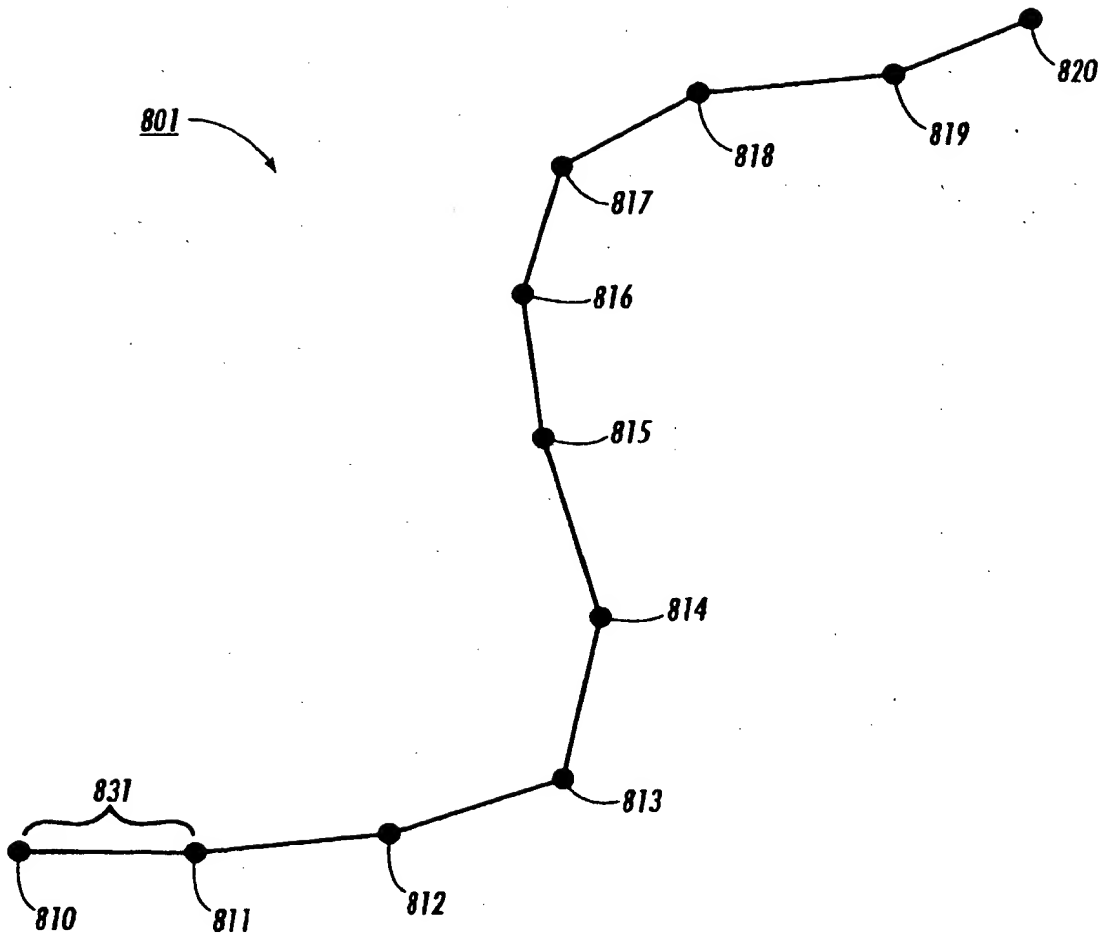




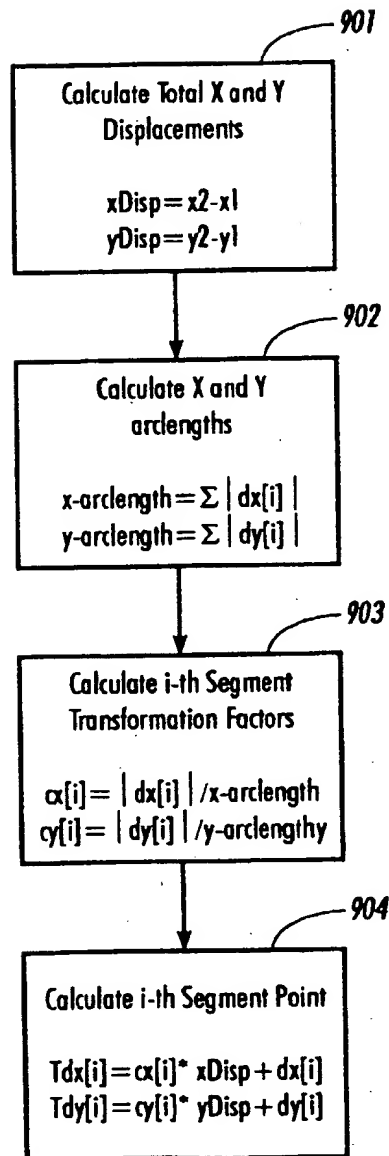
**FIG. 6**



**FIG. 7**



**FIG. 8**

**FIG. 9**

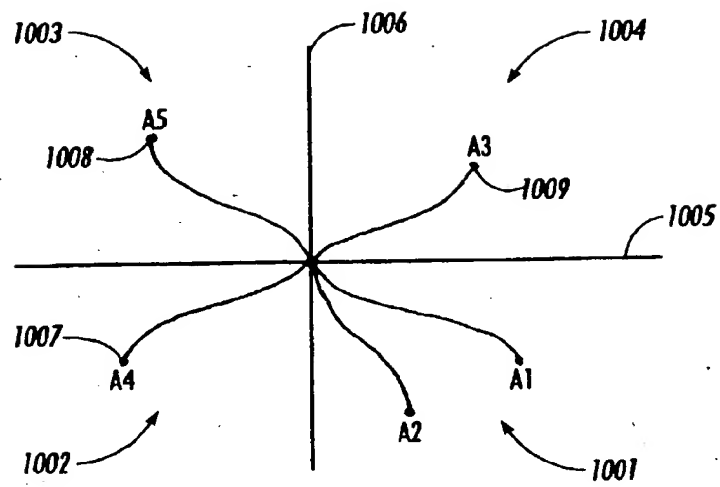


FIG. 10

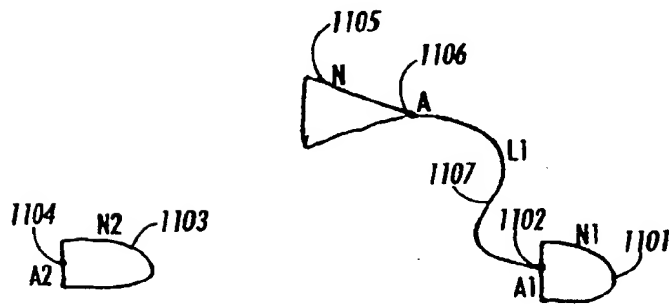


FIG. 11

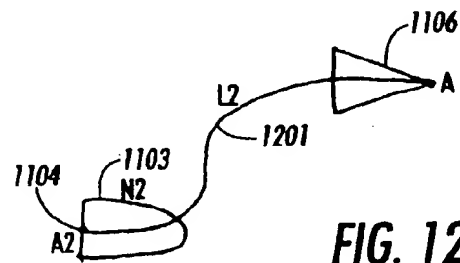
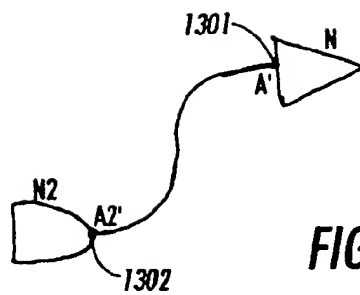
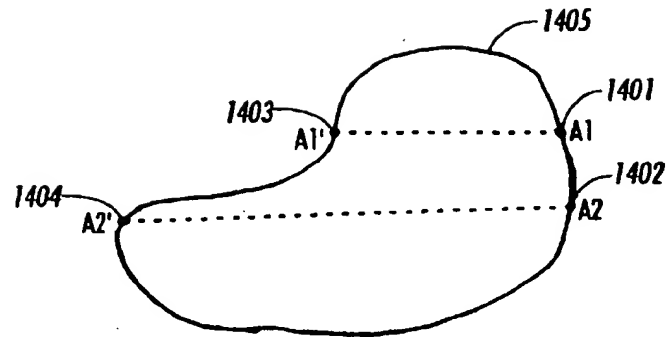


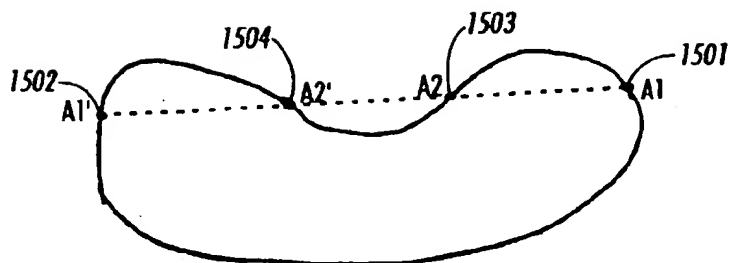
FIG. 12



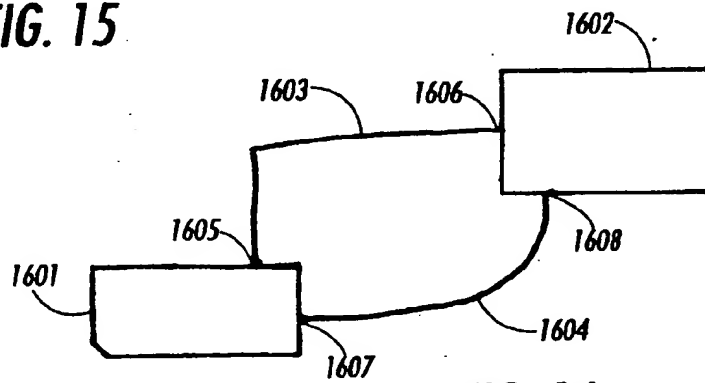
**FIG. 13**



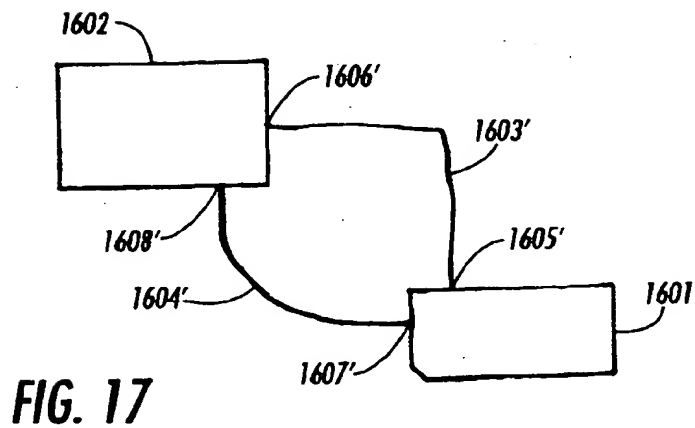
**FIG. 14**



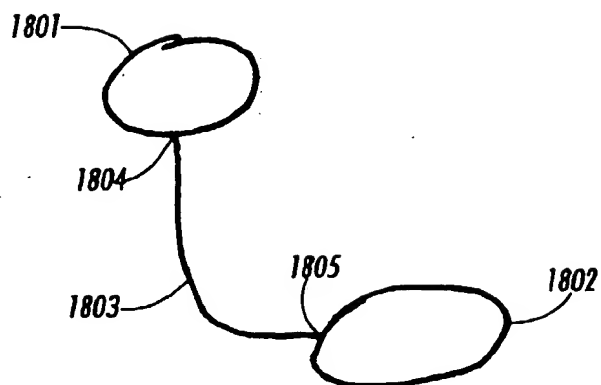
**FIG. 15**



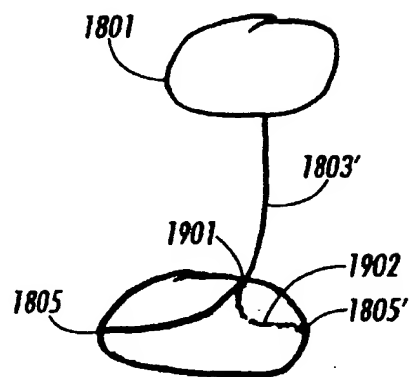
**FIG. 16**



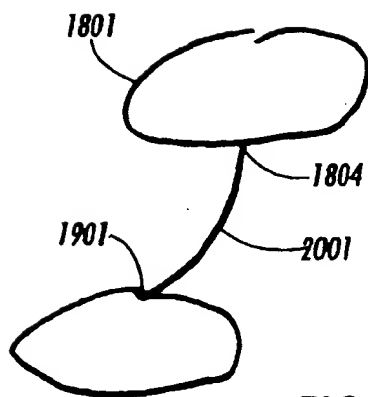
**FIG. 17**



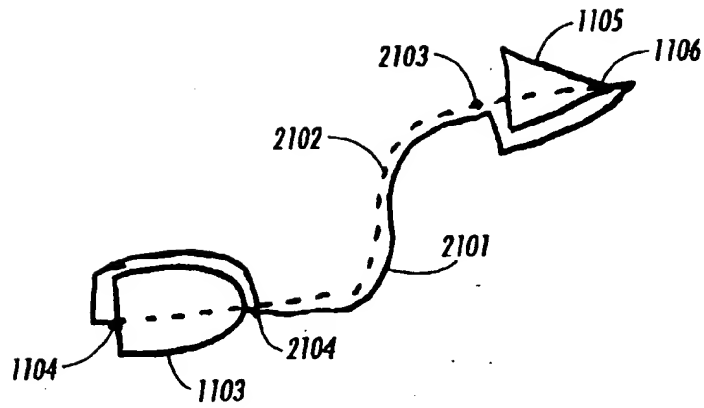
**FIG. 18**



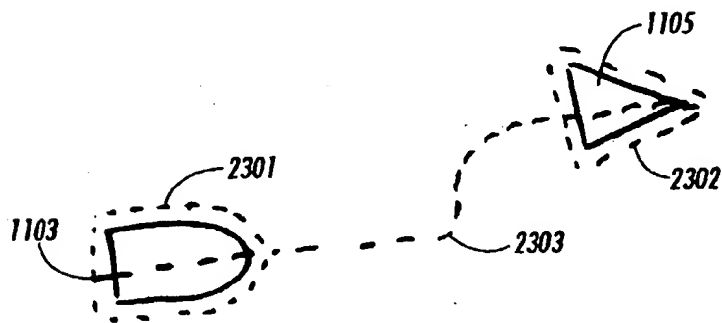
**FIG. 19**



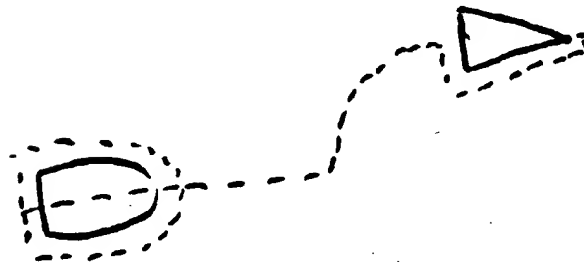
**FIG. 20**



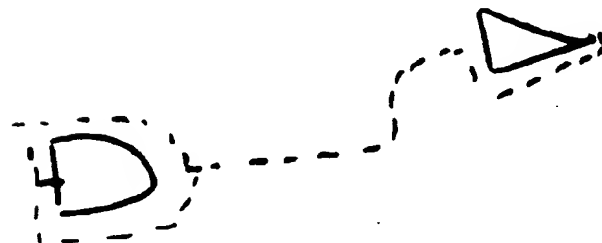
**FIG. 21**



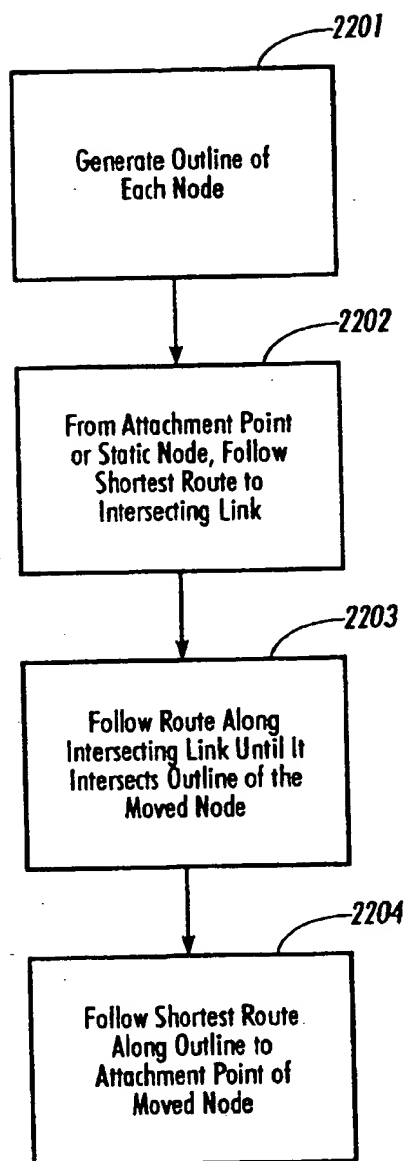
**FIG. 23**



**FIG. 24**

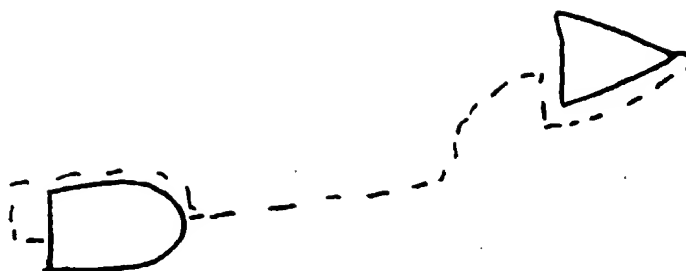


**FIG. 25**

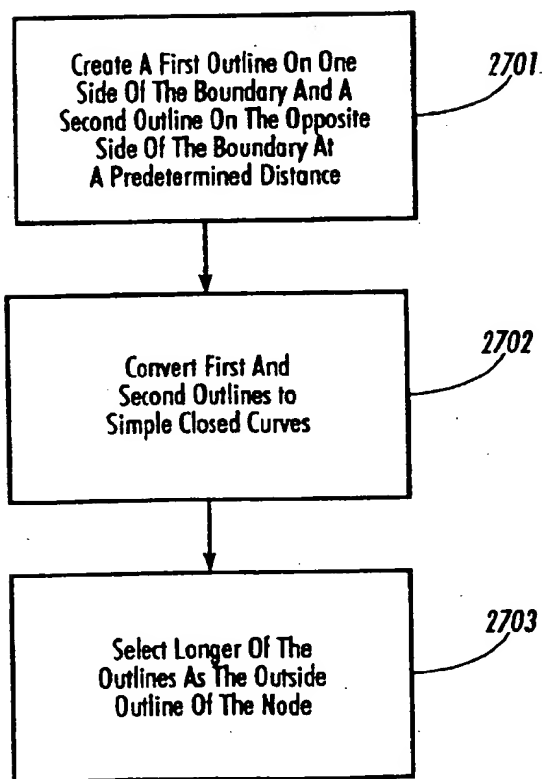


**FIG. 22**





**FIG. 26**



**FIG. 27**

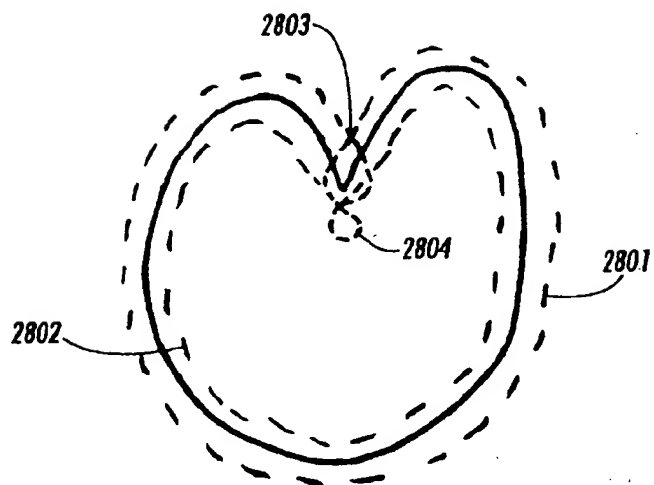


FIG. 28

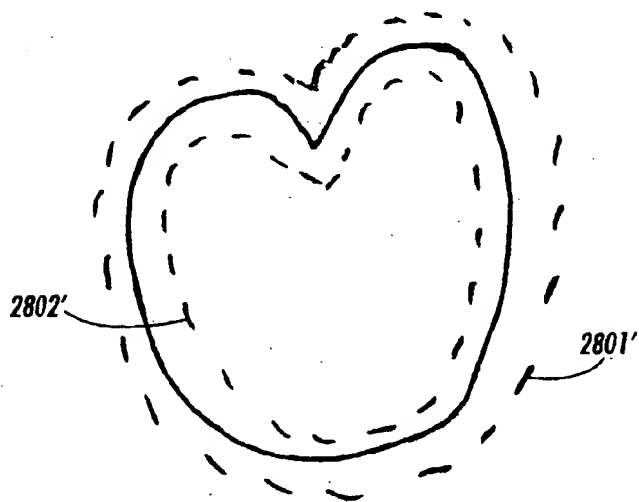


FIG. 29

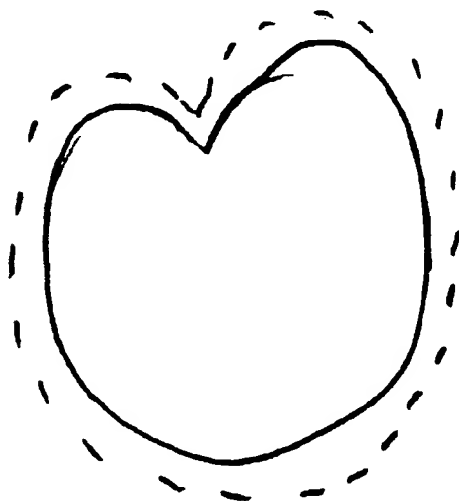


FIG. 30

(19)



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(11)

EP 0 825 559 A3

(12)

## EUROPEAN PATENT APPLICATION

(88) Date of publication A3:  
25.08.1999 Bulletin 1999/34

(51) Int Cl.<sup>6</sup>: G06T 11/20

(43) Date of publication A2:  
25.02.1998 Bulletin 1998/09

(21) Application number: 97306168.2

(22) Date of filing: 13.08.1997

(84) Designated Contracting States:  
AT BE CH DE DK ES FI FR GB GR IE IT LI LU MC  
NL PT SE  
Designated Extension States:  
AL LT LV RO SI

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## (54) Method and apparatus for modifying a node-link diagram

(57) In a computer controlled display system capable of supporting free form graphical input, techniques for maintaining the topology of a node-link structure when nodes are moved (401). When a node is moved, arbitrarily shaped links to other nodes will automatically be reshaped. The manner in which links are reshaped will depend on where a node is moved relative to the node to which it is linked. Various techniques for reshaping the node in order to retain the node-link structure topology are provided. A link may be reshaped (404, 406) by curve transformation or flipping the link shape about an axis (405). Curve transformation is a technique wherein the shape characteristics of a link are retained no matter where the node is moved. However, links that intersect, i.e. pass through, the nodes may arise from such reshaping. Various techniques for correcting link intersection situations and include flipping the attachment points (409) of the links on the nodes, truncating (412) and reattaching the link at the point where a link intersects a node or rerouting the link (410) so that intersection is avoided.

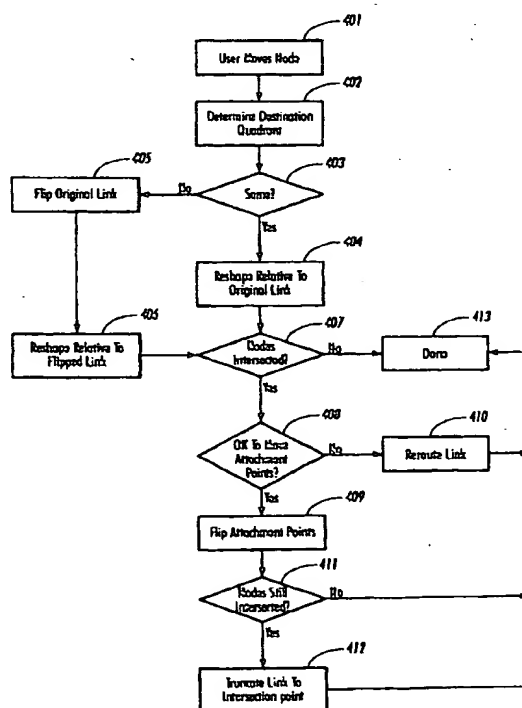


FIG. 4



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# EUROPEAN SEARCH REPORT

Application Number  
EP 97 30 6168

DOCUMENTS CONSIDERED TO BE RELEVANT			
Category	Citation of document with indication, where appropriate, of relevant passages	Relevant to claim	CLASSIFICATION OF THE APPLICATION (Int.Cl.6)
Y	WO 96 10231 A (MICROGRAFX INC) 4 April 1996 * page 26, line 1 - line 5 * * page 27, line 10 - page 28, line 28 * * claims 7.20 *	1	G06T11/20
X	* page 29, line 5 - page 20, line 10; figures 8,9 *	10	
A	---	2	
Y	"LAYOUT ALGORITHM FOR COMPUTER NETWORK GRAPHICS" IBM TECHNICAL DISCLOSURE BULLETIN, vol. 30, no. 12, 1 May 1988, pages 268-277, XP000118844 * page 268, line 7 * * page 272, line 1 - line 6; figure 5 * * page 276, paragraph 1 - paragraph 2 *	1	
A	---	3,5,7,10	
A	SAUND E ET AL: "PERCEPTUAL ORGANIZATION IN AN INTERACTIVE SKETCH EDITING APPLICATION" PROCEEDINGS OF THE FIFTH INTERNATIONAL CONFERENCE ON COMPUTER VISIO, CAMBRIDGE, MA., JUNE 20 - 23, 1995, no. CONF. 5, 20 June 1995, pages 597-604, XP000557418 INSTITUTE OF ELECTRICAL AND ELECTRONICS ENGINEERS * page 599, column 2, last paragraph - page 600, column 1, paragraph 1 * * page 602, left-hand column; figure 7 *	2-4,9	TECHNICAL FIELDS SEARCHED (Int.Cl.6) G06T
A	US 4 953 106 A (VO KIEM-PHONG ET AL) 28 August 1990 * column 9, line 1 - line 16 * * claim 1; figures 9-16 *	2,3,6	
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	-/--		
The present search report has been drawn up for all claims			
Place of search THE HAGUE		Date of completion of the search 2 July 1999	Examiner Diallo, B
CATEGORY OF CITED DOCUMENTS		T: theory or principle underlying the invention E: earlier patent document, but published on, or after the filing date D: document cited in the application L: document cited for other reasons A: technological background N: non-written disclosure I: intermediate document 3: member of the same patent family, corresponding document	
X: particularly relevant if taken alone Y: particularly relevant if combined with another document of the same category A: technological background N: non-written disclosure I: intermediate document			

EP 0 825 559 A3 (1999.07.02)



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Office

## EUROPEAN SEARCH REPORT

Application Number  
EP 97 30 6168

DOCUMENTS CONSIDERED TO BE RELEVANT			
Category	Citation of document with indication, where appropriate, of relevant passages	Relevant to claim	CLASSIFICATION OF THE APPLICATION (Int.Cl.6)
A	US 5 337 404 A (HERVE JEAN-CLAUDE ET AL) 9 August 1994 * abstract * * column 12, line 13 - column 14, line 66; claims 1-3,5; figures 8,15,20 *	1-10	
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